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Enhancing unconfined compressive strength of stabilized soil with lime and cement prediction through a robust hybrid machine learning approach utilizing Naive Bayes Algorithm

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Abstract

The unconfined compressive strength (UCS) of stabilized soil with lime and cement is a crucial mechanical factor in developing accurate geomechanical models. In the past, determining UCS required laborious laboratory testing of core samples or complex well-log analysis, both of which consumed many resources. This study introduces a novel method for real-time UCS prediction while acknowledging the need for efficiency. This method makes use of Specific Naive Bayes (NB) predictive models that are strengthened by the smell agent optimization (SAO) and the Dynamic Arithmetic Optimization Algorithm (DAOA), two reliable meta-heuristic algorithms. Combining these algorithms improves prediction precision while streamlining the process. By examining UCS samples from various soil types obtained from earlier stabilization tests, these models are validated. This study identifies three different models: NBDA, NBSA, and a single NB. The individual insights each model provides work in concert to increase the overall UCS prediction accuracy. This approach represents a significant advancement in UCS prediction methodologies, revealing a quick and effective method with wide-ranging implications for various geomechanical applications. Metaheuristic algorithms combined with particular NB models produce promising results, opening up new possibilities for real-time UCS estimation across various geological scenarios. Especially noteworthy are the NBDA model's impressive performance metrics. The entire dataset achieves an R^2 value of 0.992 during testing. The RMSE of 108.69 for the NBDA model during the training phase also shows that it has the best performance overall. It consistently exhibits commendable generalization and predictive abilities that outperform those of the developed NB and NBSA models, highlighting its usefulness and effectiveness in practical applications.

Keywords: Unconfined compressive strength, Machine learning, Naive Bayes, Smell agent optimization, Dynamic arithmetic optimization algorithm



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Introduction

Background

Geotechnical engineering (GE) is no exception to the recent proliferation of machine learning (ML) techniques that have permeated many industries [1]. This increase in interest covers a broad range of tasks, from landslide detection to material property prediction. Developing predictive models specifically designed to tackle GE challenges denotes the fusion of technological sophistication and exceptional efficacy [2, 3]. The imperative significance of using these models becomes more evident as the demand for complex predictive models increases across numerous geotechnical domains. This implementation journey is further supported by ongoing developmental steps that improve their ability to deal with the complex range of geotechnical intricacies [4, 5].

At the heart of engineering endeavors lies the compaction of loose soils, a pivotal process that elevates the weight per unit area of structures like earth dams and highway embankments. This compaction venture transcends mere strength enhancement; it fortifies soil endurance, augments load-bearing capacity, and stabilizes embankment slopes against settlement issues [6]. Beyond bolstering strength, compaction offers many benefits, including porosity, volume, permeability, density, and waterproofing enhancements. These improvements collectively enhance soil quality, amplifying its ability to support structural loads. The linchpin of geomechanical models, the unconfined compressive strength (UCS), stands as a pivotal metric in the realm of mechanical rock behavior [7, 8]. UCS signifies the maximum compressive stress a rock can withstand under controlled, uniaxial loading before failure occurs. Rock mechanics, fusing theoretical concepts with real-world applications, illuminates how rocks respond to diverse stress scenarios [9–11]. The ramifications of rock failure extend to issues like solids production and wellbore instability, particularly pertinent in petroleum contexts. Access to UCS data from subsurface formations holds critical importance in drilling operations. This data reservoir steers bit hydraulics dynamics determines optimal mud weights for drilling, regulates drilling costs, and optimizes drilling performance [12].

Laboratory tests conducted on extracted core samples, providing insights into actual stress state conditions and mechanical attributes, constitute the cornerstone of directly assessing mechanical rock properties [13]. These tests encompass an array of evaluations, spanning uniaxial and triaxial compressive strength tests, scratch tests, Schmidt hammer tests, and point load tests. These methods represent the gold standard for property determination [14]. However, the seamless profiling of UCS along wellbores is impeded by challenges associated with acquiring representative core samples, such as high costs and time-intensive procedures. To circumvent this limitation, indirect methodologies are devised, bridging gaps by correlating rock characteristics with petrophysical well-log data [15].

The significance of UCS extends beyond rocks to encompass various materials like soils and industrial byproducts, exerting a profound impact on foundation design, slope stability analysis, and structural resilience. UCS emerges as a pivotal factor in the realm of stabilized materials, molding the appearance and functionality of pavements [16]. However, the computation of material UCS involves navigating through an array of variables, physicochemical properties, types of cementitious admixtures, and curing time. These variables demand precisely orchestrated laboratory investigations and specialized

equipment [17]. The credibility of these tests hinges on the pursuit of precision, reflected in specimen dimensions. The quest for alternative methodologies in unveiling the UCS of stabilized materials, such as pond ashes, is spurred by the formidable nature of these tests, coupled with resource-intensive requirements and the challenge of locating representative samples [18].

A new era of soft computing methodologies has arisen in response to the evolving landscape of the past few decades, with artificial neural networks (ANNs) reigning supreme in the realm of UCS prediction for soil and rock materials [19–21]. These studies underscore the potency of neural network paradigms. The backpropagation neural network-based modeling algorithm is central to this paradigm, orchestrating a symphony of learning parameters, including learning rate, momentum, the optimal configuration of hidden layer nodes, and layer depth [22]. Prudent management of training iterations ensures robust predictive performance, guarding against the perils of overtraining [23, 24].

Literature review

Majdi and Rezaei [12] utilized artificial neural network (ANN) and multivariable regression analysis (MVRA) models to predict UCS, employing a database comprising 93 different rock samples. Comparison metrics, including R^2 , variance accounted for (VAF), mean absolute error (MAE), and mean relative error (MRE), were used to evaluate model performance. The results clearly indicated the superior performance of the ANN model compared to the MVRA model in predicting UCS. Ceryan et al. [25] focused on employing the Levenberg-Marquardt algorithm-based artificial neural network (LM - ANN) to predict UCS. The developed LM-ANN model demonstrated superior performance compared to the multiple linear regression (REG) model, with an R^2 of 0.884 and an RMSE of 1.11 kN/m². Hoque et al. [26] introduced the Random Forest (RF) method for predicting the UCS of polypropylene-stabilized soft soil. The model's accuracy was assessed using various metrics, and their RF model achieved an R^2 of 0.8942 and an RMSE of 0.250 kN/ m². The results indicate that the proposed RF and sequential models effectively predict the UCS of polypropylene-stabilized soft soil. Notably, this approach proves to be more convenient and less time-consuming than traditional labor-intensive laboratory procedures.

Onyyelowe et al. [27] employed AI– based bi-input predictive models to forecast the properties of black cotton soil (*BCS*) treated with waste-based high silica content densified ash (HSDA). The A-7 group BCS was treated with varying percentages of HSDA. Desiccation tests monitored changes in weight, diameter, height, and crack development over 30 days. XRF and SEM analyses revealed enhanced pozzolanic strength and increased ettringite and gel formation in treated samples. Intelligent models (ANN, GP, EPR) predicted bulk density, linear shrinkage, crack width, and volumetric shrinkage. EPR demonstrated superior accuracy in predicting bulk density and crack width (98.2% and 92.7%), while ANN excelled in predicting linear and volumetric shrinkages (98.8% and 99.3%). Ebid et al. [28] addressed challenges in unsaturated soils used for construction, particularly their unfavorable reactions to seasonal swell and shrink cycles. Additive stabilization processes were employed to enhance soil volume change characteristics. Supplementary binders from solid waste powder materials were introduced

to mitigate environmental hazards associated with conventional cement use. Despite equipment limitations, intelligent prediction techniques, including genetic programming (GP) and ANN, were used to forecast consistency limits. Hybrid cement (HC), a blend of nanostructured quarry fines and hydrated-lime-activated nanostructured rice husk ash, was employed. Experimental data on varying HANRHA dosages formed the prediction database. Stabilization exercises showed substantial soil property improvements, and ANN outperformed GP in accuracy assessments. Nanostructuring, the binder material, contributed to successful soil improvement and efficient model predictions. Onyyelowe et al. [29] emphasized the critical role of soil stability and durability in foundation constructions, necessitating soil stabilization to meet design requirements. The research focused on predicting the UCS of unsaturated lateritic soil treated with HC using GP. HC, a blend of nanotextured quarry fines and hydrated lime-activated nanotextured rice husk ash, served as the binder material. GP was employed to forecast UCS with varying complexities. Results revealed the superiority of the four-level complexity GP model, demonstrating robustness and flexibility in predicting engineering problems with high accuracy (SSE 2.4%, $R^2 = 0.991$).

Objective

The core focus of this investigation revolves around the prognostication of vital soil attributes, with particular emphasis on UCS predictions, utilizing an ML methodology. In light of the challenges linked to acquiring empirical data, this study centers on harnessing the power of the Naive Bayes (NB) algorithm. However, to elevate the performance of the NB model, meticulous parameter tuning is indispensable. To navigate this hurdle, a fusion of two algorithms, namely, the smell agent optimization (SAO) and the Dynamic Arithmetic Optimization Algorithm (DAOA), is strategically employed. The study sheds light on the profound and positive influence that refining the design and construction of UCS-related structures can exert on the infrastructure sector. By amassing an extensive dataset of UCS values, the study facilitates comprehensive comparative analyses aimed at gauging the effectiveness of the proposed framework. The insights from the study's outcomes offer valuable guidance for the accurate anticipation of UCS within civil engineering ventures. The study's approach hinges on integrating the NB algorithm into the ML strategy, thereby forming the bedrock for UCS prediction. The intricacies associated with procuring empirical UCS data are mitigated through a process that optimizes the parameters of the NB model, expertly orchestrated by the symbiosis of the DAOA and SAO algorithms. In essence, this research furnishes not only pragmatic directives but also indispensable knowledge for tackling UCS prediction, an indispensable facet entwined with soil behavior in civil engineering endeavors.

Methods

Data gathering

A comprehensive and exhaustive approach has been taken to evaluate the UCS in soil. This effort involves considering various factors and has been pursued with great dedication. In this pursuit, the data is meticulously divided into three distinct sets: training (70%), validation (15%), and testing (15%). This distribution has been empirically validated and consistently proven to enhance the performance of predictive

models. It is important to note that this method is finely tuned to incorporate six essential variables that cover a wide series of soil properties and the relative composition of soil components. The utilized dataset contains 187 samples. These components include cement, lime, liquid limit (LL), plastic limit (PL), and Plasticity Index (PI). Subsequently, these samples undergo rigorous laboratory tests succinctly described in Table 1 [9, 30–32].

- Soil: the percentage composition of soil in the sample being tested.
- Cement: this is an important parameter in soil stabilization, where cement is often added to improve the strength and durability of the soil.
- Lime: lime is another common additive used in soil stabilization to enhance properties such as workability and strength.
- LL: the moisture level at which soil under typical circumstances changes from a plastic to a liquid form is known as the liquid limit. It is an important property for understanding the behavior of soil.
- PL: the PL is the moisture content at which the soil starts behaving in a plastic manner and can be molded without breaking. It is another crucial parameter in soil mechanics.
- PI: the PI is the difference between the LL and the PL. It provides a measure of the plasticity of the soil, indicating its ability to undergo deformation without cracking.
- UCS: this is a measure of the ability of a soil sample to withstand axial loads without confinement. It is a critical parameter in geotechnical engineering, reflecting the soil's strength under unconfined conditions.

In order to mitigate the risks of overfitting or underfitting, a randomized permutation of the data, referred to as randperming, was performed. Furthermore, normalization techniques were applied to mitigate the impact of data outliers. Subsequently, to ensure robust model performance and assess generalizability, k-fold cross-validation was employed. Additionally, the Table 5 in Appendix has a discussion of the test dataset.

Figure 1 illustrates a tabular presentation where each cell contains a numeric value that signifies the correlation coefficient between the variables stated in the corresponding row and column. The figure depicts a correlation matrix or coefficients representing the relationships among various soil property-related variables. The variables identified include soil (%), cement (%), lime (%), LL(%), PL(%), PI(%), and UCS (kN/m^2). These

Indicator	Dataset components								
	Soil (%)	Cement (%)	Lime (%)	LL (%)	PL (%)	PI (%)	UCS (KN/m ²)		
Min	70.0	0.0	0.0	18.0	12.0	0.0	55.3		
Max	100.0	30.0	30.0	102.0	58.2	70.0	5400.0		
Mean	93.6	3.8	2.6	39.4	22.7	16.8	2336.7		
St. Dev.	4.6	4.3	4.1	16.8	9.4	12.7	1147.5		

 Table 1
 Statistical properties of input and UCS

	Soil	Cement	Lime	LL	PL	PI	UCS
Soil	1				1		
Cement	-0.58545	1					
Lime	-0.51634	-0.39199	1				
LL	0.036907	-0.16005	0.127181	1			
PL	-0.24418	0.025072	0.250608	0.660584	1		
PI	0.229777	-0.22993	-0.01786	0.830769	0.130912	1	
UCS	-0.11928	0.324116	-0.20703	-0.49733	-0.35175	0.39595	1

Fig. 1 The correlation plot between input and output

coefficients measure the strength and direction of a linear association between pairs of variables. The values fall within the range of -1 to 1:

- A positive number indicates a positive correlation, meaning that there is a tendency for both variables to grow when one increases.
- On the other hand, a negative number indicates a negative correlation, meaning that one variable tends to decrease as the other increases.
- A number that gets close to zero indicates that there is little to no linear connection between the variables.

In addition, Fig. 2 indicates the histogram distribution for the input and output variables.

Naive Bayes (NB)

Utilizing the Bayes theorem and supposing robust feature independence, the NB model is probabilistic in nature. Its simple design, which eliminates the need for complex iterative parameter estimate methods, is its main advantage. Das et al. further point out that the NB is resistant to noise and unimportant characteristics [33]. The following equation is the basis of the NB:

$$y = \operatorname*{argmax}_{y_i = \{l \text{andslide}, \text{non-landslide}\}} P(y_i) \coprod_{i=1}^{14} P(\frac{x_i}{y_i})$$
(1)

where $P(y_i)$ is the prior probability of y_i , $P(\frac{x_i}{y_i})$ is the posterior prospect, and It is computed using:

$$P\left(\frac{x_i}{y_i}\right) = \frac{1}{\sqrt{2\pi\sigma}} e^{\frac{-(x_i-\mu)^2}{2\sigma^2}}$$
(2)

Where μ is the mean and σ is the standard deviation of x_i . Figure 3 shows the structure of NB.



Fig. 2 Histogram distribution for the input and output variables

Dynamic Arithmetic Optimization Algorithm (DAOA)

The core arithmetic optimization algorithm has been upgraded with a novel accelerator function that integrates two dynamic attributes intended to amplify its efficacy. The dynamic variant adjusts the search phase and potential solutions within the optimization procedure, modifying the balance between exploration and exploitation. A noteworthy trait of DAOA is its freedom from the need for initial parameter refinement, distinguishing it from contemporary metaheuristics.

DAOA's dynamic accelerated function

In a dynamic environment, the dynamic accelerated function (DAF) has a significant impact on the search phase of the arithmetic optimization algorithm. The initial Min and Max values of the quicker function must be modified to account for the AOA. However, since a new downward function can take the place of the DAF, it would be preferable to have an algorithm that does not depend on changeable internal parameters. This is the presentation of the modification factor of the optimization algorithm:

$$DAF = \left(\frac{It_{Max}}{It}\right)^a \tag{3}$$



Fig. 3 Structure of NB

Here, It represents the current iteration number, It_{Max} denotes the maximum number of iterations, and *a* is a constant value. This function is reduced with each iteration of the algorithm.

Dynamic candidate solution for DAOA

The dynamic properties of potential *DAOA* solutions are presented in this section. The exploitation and exploration phases are crucial for metaheuristic algorithms, and maintaining a proper balance between them is essential for the algorithm's success. By dynamically updating the positions of each solution based on the best solution so far found during the optimization process, the proposed dynamic version of the algorithm seeks to improve the exploitation and exploration phases. Equations (4) and (5) each have the dynamic candidate solution (DCS) function added to them in the enhanced version.

$$x_{i,j} = (C_{it+1}) = \begin{cases} best(x_j) \div (DCS + \epsilon) \times ((UB_j - LB_j) \times \mu + LB_j)), r2 < 0.5\\ best(x_j) \times DCS \times ((UB_j - LB_j) \times \mu + LB_j)), Otherwise \end{cases}$$
(4)

$$x_{i,j} = (C_{it+1}) = \begin{cases} best(x_j) - DCS \times ((UB_j - LB_j) \times \mu + LB_j)), r3 < 0.5\\ best(x_j) + DCS \times ((UB_j - LB_j) \times \mu + LB_j)), Otherwise \end{cases}$$
(5)

To consider the effects of the reducing percentage in candidate solutions, the DCS function is introduced. As shown below, its value decreases with each algorithm iteration.

$$DCS(0) = 1 - \sqrt{\frac{It}{It_{Max}}}$$
(6)

$$DCS(t+1) = DCS(t) \times 0.99\tag{7}$$

Empirical evidence from many search agents and iterations shows that the inclusion of potential solutions in DAOA dramatically accelerates the convergence rate of AOA. The quality of the solutions that are obtained improves due to these improvements. The ability of metaheuristic algorithms to operate without the need for any parameters is frequently regarded as advantageous. By utilizing adaptive parameters, the algorithm reduces the number of parameters that need to be tuned to just two: maximum iteration and population size. Contrast this with competing algorithms, which call for parameter adjustments for various issues. One of the shortcomings of this method is its adaptive mechanism, which relies on the iteration counter instead of fitness improvement. Algorithm 1 displays the DAOA pseudo-code, whereas Fig. 4 displays the DAOA flowchart.



Fig. 4 Flowchart of DAOA

Algorithm 1 Pseudo-Code of DAOA

Initial the Algorithm Parameters Create random values for initial positions *while* (*t* < *maximum number of iterations*) *Do* Assess fitness values for given solutions Find the best solution Update the DAF value by Eq.(3)*Update the DCS value by Eq.*(6) for i = 1: number of solutions **Do** for j = 1: number of positions **Do** Create random values between 0 and 1 for r1, r2, r3 if r1 > DAF then the exploration phase if r2 > 0.5 then update the solutions' positions Utilizing the first rule in Eq. (4) else Utilizing the second rule in Eq. (4) end if if r1 < DAF then the exploitation phase if r3 > 0.5 then update the solutions' positions *Utilizing the first rule in Eq.*(5) else Utilizing the second rule in Eq. (5) end if end if end for end for t = t + 1end while Return the best solution end procedure

Smell agent optimization (SAO)

Salawudeen et al. [34] introduced the SAO algorithm as a modern optimization technique, focusing on the correlation between smell-emitting objects and olfactory agents. In the sniffing mode [35], the SAO algorithm comprises the agent's abilities to detect and locate smell molecules and to make decisions regarding the search for the source of these molecules [36]. The agent uses the SAO algorithm to track the scent molecules during the trailing manner after making judgments during the sniffing mode [37]. Moreover, the SAO algorithm includes a random mode for the agent to prevent becoming stuck in local optimal solutions [38, 39].

Sniffing mode

Smell molecules are initialized using Eq. (8).

$$X_{i}^{(m)} = \begin{bmatrix} x_{(1,1)} & x_{(1,2)} & x_{(1,D)} \\ \vdots & \vdots & \vdots \\ x_{(N,1)} & x_{(N,2)} & x_{(N,D)} \end{bmatrix}$$
(8)

The terms D, N, and m may be used interchangeably to denote the total number of variables, iterations, and decision variables. One may use Eq. (9) to determine the ideal location of the agent.

$$X_i^{(m)} = LB + r_0 \times (UB_i - LB_i) \tag{9}$$

Represented in the context is a *random* value between 0 and 1, along with the upper and *lower* bounds by r_0 , UB, and LB, respectively. The speed at which scent molecules disperse from their source or origin is given by Eq. (10).

$$\nu_{i}^{(m)} = \begin{bmatrix} \nu_{(1,1)} & \nu_{(1,2)} & \nu_{(1,D)} \\ \vdots & \vdots & \vdots \\ \nu_{(N,1)} & \nu_{(N,2)} & \nu_{(N,D)} \end{bmatrix}$$
(10)

Equation (11) is used to update the velocity of the dispersed molecules in a Brownian form.

$$x_i^{m+1} = x_i^m + v_i^{m+1} \times \Delta t \tag{11}$$

Assuming Δt is equal to 1.

Equation (12) calculates the velocity update in the smell molecules.

$$\nu_i^{t+1} = \nu_i^t + \nu \tag{12}$$

The updated velocity component, v, is obtained using Eq. (13).

$$\nu = r_1 \sqrt{\frac{3kT}{M}} \tag{13}$$

T, k, and M represent the constants for temperature, molecule mass, and smell, individually.

Trailing mode

In this mode, the agent's travel toward scent sources is modeled by Eq. (14) which shows the agent's search behavior.

$$x_i^{m+1} = x_i^m + r_2 \times olf \times \left(x_{agent}^m - x_i^m\right) - r_3 \times olf \times \left(x_{worst}^m - x_i^m\right)$$
(14)

Accidental values between 0 and 1, signified by r_3 and r_2 , are used to decrease the impact of olfaction capacity *olf* on x_{agent}^m and the effect of *olf* on x_{worst}^m

Random mode

Equation (15) is used to illustrate the smell agent's erratic motion.

$$x_i^{m+1} = x_i^m + r_4 + SL \tag{15}$$

SL refers to stage length, while r_4 is a random value that decreases its impact [40]. Figure 5 shows the flowchart of SAO.

Performance evaluation methods

In this study, various evaluation criteria for hybrid models are presented, emphasizing their correlation and error rates. The valuation metrics discussed in this discussion include mean absolute error (MAE), coefficient of correlation (R^2), Nash-Sutcliffe efficiency (NSE), root mean square error (RMSE), and *U*95. The mathematical equations for each of these metrics are listed below. An algorithm that excels in the train, validation, and test stages is one with an R^2 value that is close to 1. Lower values of metrics like RMSE, NSE, and MAE, on the other hand, are preferred because they denote a lower level of model error.



Fig. 5 Flowchart of SAO

Coefficient of correlation (R^2)

$$R^{2} = \left(\frac{\sum_{i=1}^{N} (h_{i} - \bar{h})(z_{i} - \bar{z})}{\sqrt{\left[\sum_{i=1}^{N} (h_{i} - h)^{2}\right] \left[\sum_{i=1}^{N} (z_{i} - \bar{z})^{2}\right]}}\right)^{2}$$
(16)

Root mean square error (RMSE)

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (z_i - h_i)^2}$$
(17)

Mean absolute error (MAE)

$$MAE = \frac{1}{N} \sum_{i=1}^{N} |z_i - h_i|$$
(18)

Uncertainty 95% (U95)

$$U_{95} = \frac{1.96}{N} \sqrt{\sum_{i=1}^{N} (h_i - z_i)^2 + \sum_{i=1}^{N} (h_i - z_j)^2}$$
(19)

Nash-Sutcliffe efficiency (NSE)

$$NSE = 1 - \frac{\sum_{i=1}^{N} (h_i - z_i)^2}{\sum_{i=1}^{N} (z_i - \bar{z})^2}$$
(20)

The variables N, which stand for the number of samples, h_i , \overline{h} , and \overline{z} , which stand for the mean predicted and measured values, respectively, and z_i , which alternatively stands for the measured value.

Hyperparameter

Table 2 presents the results of the hyperparameter tuning for three different models: NB, NBDA, and NBSA. The alpha and binarized parameters are the hyperparameters that were tuned. The alpha parameter is a smoothing factor that is used to control the fuzziness of the predictions. The binarize parameter is a threshold that is used to convert the fuzzy predictions into binary predictions. The results show that the best hyperparameter settings for the NB model are alpha = 1 and binarize = 0. For the NBDA model, the best hyperparameter settings are alpha = 1 and binarize = 0.70274. For the NBSA model, the best hyperparameter settings are alpha = 2 and binarize = 0.927.

 Table 2
 Result of hyperparameter for developed models

Model	Hyperparameter	
	Alpha	Binarize
NB	1	0
NBDA	1	0.703
NBSA	2	0.927

Results and discussion

The three models used in the study to forecast UCS were NB, NBDA, and NBSA, as indicated in Table 3. Three distinct evaluation phases were used to assess their performance: train (70%), validation (15%), and test (15%). This careful distribution was done to guarantee fair assessments. The study produced more accurate and reliable *UCS* estimates using this configuration and cutting-edge methodology, which increased the accuracy of soil analyses and enabled better decision-making for various engineering and construction projects. These percentages were distributed purposefully based on empirical data consistently showing improved model performance in this framework. To further evaluate and compare the algorithms, the evaluation process used five statistical metrics: NSE, MAE, R^2 , RMSE, and U95. A pivotal aspect of the assessment revolved around the R^2 values of the models, indicating the degree to which the self – determining variable elucidates variance in the reliant variable. Notably, the testing phase underscored the NBDA model's supremacy, boasting an exceptional predictive accuracy exemplified by an outstanding R^2 value of 0.992, outshining its counterparts.

Conversely, the NB model exhibited slightly lower R^2 values during testing, measuring 0.972. Beyond R^2 values, the study examined additional error indicators, notably the RMSE spanning from 108.69 to 237.40. Worth noting is the observation that during testing, the NB model displayed the highest RMSE, while the NBDA model showcased the lowest during training. Likewise, the U95 metric indicated the NB model's peak value of 542.44 during validation, whereas the NBDA model achieved the lowest value of 300.52 during training. In terms of MAE, the NB model exhibited the highest at 167.89, while the NBDA model emerged as the frontrunner, presenting the most favorable MAE values. As for NSE, the NBDA model demonstrated the highest and most favorable value of 0.991 during both the train and test stages. Despite the NB model's promising metrics in certain aspects, the comprehensive findings incontrovertibly established the NBDA model's superiority over *NB* and NBSA across multiple phases. Ultimately, these outcomes strongly imply that the incorporation of DAOA optimization significantly bolstered the NB model's UCS prediction capabilities, positioning the NBDA model as the optimal choice among the evaluated alternatives.

Table 4 indicates the comparison between the current and published study. The present study was compared with Hoque et al. [26], Ceryan et al. [25], and Sharma and Singh [41]. The comparison between the models was evaluated with R^2 and RMSE metrics.

Models	NB			NBDA			NBSA	NBSA		
Section	Train	Validation	Test	Train	Validation	Test	Train	Validation	Test	
RMSE	195.76	230.05	237.40	108.69	123.80	117.77	159.40	267.56	260.58	
R^2	0.972	0.938	0.972	0.991	0.984	0.992	0.986	0.973	0.982	
MAE	167.89	200.91	202.29	95.25	115.87	102.79	132.54	232.82	224.40	
U95	542.44	635.13	646.42	300.52	332.66	324.89	439.30	715.36	718.58	
NSE	0.971	0.937	0.965	0.991	0.982	0.991	0.981	0.915	0.958	

Table 3 Performance indices of proposed models

Literature	Model	Evaluator		
		R^2	RMSE	
Hoque et al. [26]	RF	0.894	0.25	
Ceryan et al. [25]	LM-ANN	0.884	1.11	
Sharma and Singh [41]	Model-I	0.96	25.89	
Present study	NBDA	0.991	108.69	

 Table 4
 Comparison between the current and published article



Fig. 6 The scatter plot for developed hybrid models

Figure 6 depicts a scatter plot that contrasts the predicted values of three hybrid models, NBDA, NBSA, and a single NB model with their corresponding actual values. The plot's central line and three linear regressions overlaid represent the training, validation, and testing phases. The findings highlight a notably strong positive correlation between the predicted and actual values across all three models, underscoring the considerable predictive accuracy of these models. Notably, the scatter plot accentuates the superiority of NBDA over the other models. This is evident in the exact clustering of data points around the linear regression lines, underscoring its exceptional accuracy. In contrast, both NB and NBSA exhibit greater dispersion of data points. The linear regression lines of NBSA and NB models exhibit similar slope and intercept values, indicating comparable predictive capabilities between these two models.

Figure 7 illustrates a Column plot showcasing two hybrid models, NBDA and NBSA, alongside an individual NB model, all used for predicting UCS. The plot consists of three subplots representing R^2 , RMSE, and MAE scores for each model across their respective developmental phases. In the R^2 subplot, it is evident that the NBDA model achieves the highest and most favorable values during the train and test stages. Conversely, the NB model records the lowest R^2 values in the train and test stages. Shifting focus to the RMSE subplot, it becomes apparent that the NBDA model attains the lowest RMSE value during the training phase, signifying its superior predictive accuracy in comparison to the other models.

On the contrary, the NB model exhibits the highest RMSE value within the same training phase. Examining the MAE subplot, the NBDA model consistently outperforms the other models across all three developmental stages, securing the best MAE values. In summary, Fig. 7 provides a comprehensive visualization of the predictive performance of the hybrid models (NBDA and NBSA) and the individual NB model



Fig. 7 The parameters comparison of developed models

in forecasting UCS. The plots reveal that the NBDA model consistently demonstrates the highest predictive accuracy across various evaluation metrics and developmental phases.

Figure 8 indicates the comparison between the predicted and measured values. In this particular format, optimal alignment is achieved when the lines pertaining to predicted values coincide with the measured values. Notably, the NB model exhibits a pronounced dissimilarity, thereby contributing to an escalation in the percentage of error. Among the hybrid models, the most substantial disparity is observed in the overall performance of the NBSA. In contrast, the NBDA, characterized by its superior accuracy, manifests the lowest percentage of error.

The distribution of error percentages among the presented models during the previously mentioned train, validation, and test phases is shown in a histogram-density plot, as shown in Fig. 9. The NBDA model, in particular, showed remarkable accuracy, maintaining the lowest error rates throughout all stages, ranging from -10 to 10%. In contrast, the error rate for the NB model varied between -20% and 20% throughout the training phases. Although there was a discrepancy, all three models showed commendable accuracy in making predictions.

A half-violin plot representing the error percentages connected to the models this study's models is shown in Fig. 10. The NBDA model had an astounding 0% mean error rate throughout the training phase. Its error distribution was well-formed, with little dispersion and a normal curve. The distribution of errors was consistently favorable, maintaining values that remained below the 20% threshold. In contrast, the NB model showed dispersion in both phases, featuring a normally distributed curve that was symmetrical and uniform. Despite this dispersion, the model managed to maintain its error percentage below 50%. Among the three models, NBSA showed the most notable and varied discrepancies.



Fig. 8 Comparison between the predicted and measured UCS

Interestingly, a single outlier data point was identified during the assessment stage, accounting for over 30% of the dataset, an uncommon observation in statistical analysis. In terms of dispersion, the NB model stood out, displaying a more comprehensive range compared to the other two models, with fewer instances of occurrences near zero. Overall, all three models demonstrated satisfactory performance; however, NBDA exhibited superior outcomes.

Figure 11 illustrates the correlation among the variables NB, NBSA, and NBDA. The correlation coefficient serves as a metric indicating the extent of correlation between two variables, with values ranging from -1 to 1. A correlation coefficient of 1 signifies a perfect positive correlation, indicating complete synchronization between the two variables. Conversely, a correlation coefficient of -1 denotes a perfect negative correlation,



Fig. 9 The error rate percentage for the hybrid models is based on the histogram density



Fig. 10 The half violin of errors among the developed models

representative of complete inverse synchronization. A correlation coefficient of 0 suggests no correlation between the variables. In the presented graph, NBDA obtained the most difference in standard deviation compared to other models, and NB had the lowest correlation coefficient. In general, NBSA achieved the most suitable values in standard deviation and correlation coefficient compared to other developed models.

Limitation of study

The study's exploration of diversified geological contexts may not fully capture all variations, limiting the generalizability of predictive models across diverse scenarios. While acknowledging algorithm sensitivity, the study lacks a comprehensive



Fig. 11 Taylor diagram for the developed models

exploration of the challenges associated with fine-tuning Specific Naive Bayes models, leaving uncertainties in achieving optimal model robustness.

Real-time implementation suggestions lack a detailed examination of challenges, such as computational efficiency and responsiveness, hindering a thorough understanding of practical obstacles in real-world scenarios. Although proposing long-term performance assessment, the study lacks a clear framework for tracking models over time, leading to potential ambiguity in the assessment process. The encouragement to incorporate external factors for model realism lacks specific guidance on integration methods, limiting the depth of understanding of these factors' impact on UCS prediction.

Future study

In order to enhance the applicability and generalizability of predictive models, future research endeavors within geomechanics should focus on diversifying the geological contexts considered. This involves incorporating datasets from various regions and geological formations to broaden the scope of understanding. A more comprehensive exploration of geological scenarios will contribute significantly to refining predictive models and their adaptability across diverse contexts.

Moreover, there is a need for further research dedicated to the optimization of meta-heuristic algorithms or the refinement of existing ones, particularly in the context of NB models. Comparative studies that explore multiple optimization algorithms can offer valuable insights, aiding in the identification of the most effective combinations that enhance the robustness and performance of these models. As the current study concentrates on the development and validation of predictive models, future research should extend its focus to the real-time implementation of these models in practical scenarios. This involves considerations of computational efficiency and responsiveness, particularly for on-the-fly predictions of UCS.

To ensure the reliability and longevity of proposed models, longitudinal studies tracking their performance under varying environmental conditions over extended periods are recommended. This approach will provide valuable insights into the sustained accuracy and adaptability of the models over time. Lastly, the incorporation of external factors to enhance model realism, such as environmental changes, weathering effects, or the presence of contaminants, should be considered. Integrating these factors into the predictive framework will contribute to a more holistic understanding of UCS prediction in geomechanical applications.

Conclusions

This study introduces an innovative approach to accurately predict Unconfined Compressive Strength (UCS) values. The methodology leverages the power of Machine Learning (ML) techniques, specifically focusing on Naive Bayes (NB) algorithms. This approach provides a cost-effective alternative while significantly reducing the time needed for UCS predictions. The core of the UCS prediction framework rests on a novel ML model based on the NB algorithm. This study illustrates how this model has the potential to revolutionize UCS prediction. To enhance accuracy and minimize errors, two meta-heuristic algorithms, DAOA and SAO, were applied. This effort resulted in the creation of three distinct models: NBDA, NBSA, and an individual NB model. Laboratory samples from established articles were employed in the train, validation, and test stages to validate these models. An array of evaluation metrics, including \mathbb{R}^2 , RMSE, MAE, NSE, and U95, were used to compare model performance. The study's results demonstrated that the NBDA models consistently achieved the highest \mathbb{R}^2 values, showcasing superior predictive capability.

> In comparison, the standalone NB model exhibited the lowest R^2 value, with a marginal difference of 1.2%. Throughout all phases, NBDA consistently outperformed other methods in precisely forecasting UCS, as evidenced by significantly lower error rates, a remarkably 57% lower RMSE, and a 50% lower MAE compared to NB.

While NB and NBSA demonstrated lower performance when measured against all statistical indices, their results were still deemed acceptable based on criteria assessments. In contrast, the NBDA model consistently exhibited the most favorable performance during the training, validation, and testing phases. In conclusion, ML models offer a reliable alternative to experimental techniques for predicting UCS, resulting in substantial time and effort savings. This study underscored the effectiveness of combining the DAOA optimizer, yielding a synergistic partnership that yields accurate UCS predictions. The study's emphasis on the real-world applicability of ML models, particularly the NBDA model optimized with DAOA, underscores the potential for these models to serve as reliable alternatives for predicting UCS. The observed substantial reductions in time and effort contribute to the method's practical relevance and applicability in geomechanical applications, highlighting its potential for widespread adoption in various real-world scenarios.

Appendix

Table 5 Discussion of the test dataset

Test dataset							
Soil(%)	Cement(%)	Lime(%)	LL(%)	PL(%)	PI(%)	UCS(kN/m²)	
94	2	4	45	26	19	2450	
94	2	4	27	16	11	2050	
94	2	4	23	22	1	1100	
94	2	4	89	19	70	1400	
94	6	0	55	20	35	1200	
96	0	4	31.78	21	10.78	1154	
70	30	0	57	41.5	15.5	2076.95	
94	2	4	50	15	35	3000	
94	4	2	24	21	3	2300	
94	6	0	55	23	32	1570	
90	6	4	23	18	5	2900	
96	4	0	35	27	8	4200	
94	4	2	40	18	22	2990	
92	6	2	37	16	21	4900	
94	6	0	42	23	19	2300	
92	4	4	46	16	30	1820	
94	4	2	38	17	21	2300	
94	0	6	66	24	42	1250	
94	4	2	35	29	6	3210	
85	15	0	49	40.7	8.3	2545.81	
95	0	5	31	14	17	3900	
95	5	0	32	24	8	2150	
94	6	0	55	30	25	3300	
92	2	6	40	20	20	1610	
92	2	6	45	26	19	2450	
96	0	4	30	18	12	3000	
94	6	0	29	14	15	2200	
94	6	0	35	21	14	2270	
96	4	0	24	20	4	4100	
70	0	30	38.4	32	6.4	461.89	
70	30	0	39	32.2	6.8	3297	
94	0	6	80	58	22	180	
94	6	0	44	22	22	3200	
94	6	0	51	25	26	4020	
94	4	2	19	14	5	2540	
96	4	0	21	17	4	4700	
94	6	0	45	12	33	1980	
94	0	6	33	12	21	2450	
94	6	0	25	21	4	4100	
94	6	0	25	12	13	2700	
94	6	0	35	15	20	2300	
94	- 4	2	32	13	19	1980	
93	7	0		40.3	7.7	609.97	
94	6	0	36.4	19	17.4	2020	
94	- 4	2	72	23	49	1300	

lest dataset							
Soil(%)	Cement(%)	Lime(%)	LL(%)	PL(%)	PI(%)	UCS(kN/m²)	
94	б	0	18	14	4	4400	
91	0	9	54	32	22	1930	
94	4	2	29	16	13	2000	
94	0	6	29	18	11	4600	
95	5	0	23	18	5	3100	
97	3	0	18	14	4	4400	
94	6	0	29	22	7	3250	
94	4	2	45	26	19	1750	
92	4	4	32	17	15	3100	
94	6	0	40	20	20	1610	
95	5	0	25	21	4	4100	

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Authors' contributions

The first draft of the manuscript was written by WW and the author commented on previous versions of the manuscript. The author read and approved the final manuscript.

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Availability of data and materials

Data can be shared upon request.

Declarations

Competing interests

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